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DISCUSSION PAPER

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Cycle commuting in Belgium: Spatial determinants and 're-cycling' strategies

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Abstract

This paper attempts to explain the spatial variation of the use of a bicycle for commuting to work at the level of the 589 municipalities in Belgium. Regression techniques were used and special attention was paid to autocorrelation, heterogeneity and multicollinearity. Spatial lag models were used to correct for the presence of spatial dependence and a disaggregated modelling strategy was adopted for the northern and southern parts of the country. The results show that much of the inter-municipality variation in bicycle use is related to environmental aspects such as the relief, traffic volumes and cycling accidents. Town size, distance travelled and demographic aspects also have some effect. In addition, there are regional differences in the effects of the structural covariates on bicycle use: the impact of variables such as traffic volume and cycling accidents differs substantially between the north and the south of the country. This paper also suggests that high rates of bicycle use in one municipality stimulate cycling in neighbouring municipalities, and hence that a mass effect can be initiated, i.e. more cycle commuting encourages even more commuters in the area to cycle. These findings provide some recommendations for decision-makers wishing to promote a shift from car to bicycle use.

Keywords: cycling, commuting, spatial lag model, spatial regime, pro-cycling strategies.

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1. Introduction

Most developed countries face environmental and mobility problems as a consequence of widespread car use. Partly due to long-term trends such as the increase in per capita income, car ownership has increased substantially since 1950 (Pooley and Turnbull, 2000; Rietveld, 2001). This has induced many changes, and made our societies more car dependent, leading to the progressive development of new low-density residential estates as well as commercial and industrial activities in peripheral locations (peri-urbanisation). Individuals now have higher levels of mobility and they travel more often, over larger distances, and carry out more complex trips (i.e. they undertake several activities in one trip) (Jensen, 1999; Knowles, 2006). This has various negative impacts upon society and the environment: congestion, air pollution, noise, vibrations, health problems (e.g. due to a lack of physical activity or the inhalation of polluting agents), accidents, growing infrastructure costs, and accessibility problems for low-income groups (Dobruszkes and Marissal, 1994; EC, 2000; Kingham et al., 2001; Bergström and Magnusson, 2003; Witlox and Tindemans, 2004; Knowles, 2006; EEA, 2007).

The promotion of public transport and/or non-motorised modes of transport is intended to address such environmental and mobility problems. More particularly, cycling is a "green" alternative to commuting by car (Chapman, 2007; Woodcock et al., 2007). It is also a space-and energy-efficient mode of transport and is affordable for a large majority of households (Pucher et al., 1999; Rietveld, 2001; Gatersleben and Appleton, 2007; Woodcock et al., 2007). Thus a substantial shift from car to bicycle could reduce urban congestion as well as the environmental harm caused by air and noise pollution. Moreover, cycling to work provides health benefits (if performed on regular basis) (de Geus et al., 2008, 2009) and may help to allay some of the growing concerns about the physical inactivity (which is the second major cause of premature death in industrial countries, after tobacco (BMA, 1992; Pucher et al., 1999; WHO, 2002a, 2002b)).

In Belgium, while approximately 21% of commuters live within cycling distance (i.e. less than 5 km) of their work, and 39% make trips of less than 10 km, only 6% of all commuting trips are carried out with a bicycle as the main method of transport (Verhetsel et al., 2007). The percentage of people who live within 5 km of their work who commute by bicycle is relatively low (19%), and the majority (more than 53%) use their car. There is hence great potential for a shift from car to bicycle for short commutes. However, there are several societal, economic and environmental factors that dissuade people from cycling. These include a lack of cycling infrastructure, the topography, weather, road accidents, and company-related constraints. They need to be clearly identified to help policy makers to mitigate them and to promote bicycle use in Belgium. Such findings could then support the implementation of adequate policies in favour of a modal shift from car to bicycle commuting, at least for short distances.

Within this framework, we aimed to examine which factors have the greatest influence on bicycle use for commuting in Belgium. We therefore carried out multivariate analyses out at the scale of all 589 municipalities (the smallest administrative unit) in the country. A large set of "explanatory" variables was included in the analysis, with specific attention to environmental variables as well as demographic components. Spatial autocorrelation, heterogeneity and multicollinearity problems were diagnosed and treated, with the aim of improving the results.

The structure of the paper is as follows. A thorough review of the literature on the factors that have a potential impact on bicycle use is given in Section 2. The third section presents the spatial context. Section 4 describes the objectives of the paper and the data (dependent variable and explanatory variables) in more detail. The methodological approach used to deal with multicollinearity, heterogeneity and spatial autocorrelation is presented in Section 5. The results of the multivariate analyses are reported in Section 6. Potential pro-cycling strategies are discussed in Section 7, on the basis of the results. Finally, in Section 8, our concluding remarks underscore the importance of accounting for multicollinearity, spatial dependence and spatial heterogeneity to achieve reliable statistical inferences.

2. Identifying the main determinants of bicycle use

A large range of factors have an impact on bicycle use in commuting trips: demographic, socio-economic, societal, cultural, but also environmental and policy-related determinants act as deterrents or encourage cycling. Based on an extensive review of the literature, this section provides a short overview of these determinants.

2.1. Demographic and socio-economic determinants

Socio-economic and demographic determinants include age, income, gender, education, professional field and status, and family commitments (e.g. having young children). Young commuters (< 25 years) generally have low/medium income and often cannot afford a car, which has a clear impact on their choice. Moreover, some of them do not have a driving license and have to use public transport or non-motorised forms of transport when they travel to work. The physical abilities of individuals also depend on their age: young commuters are more likely to enjoy good physical health and to cycle more. Gender has an influence on the decision on whether or not to cycle: on average, men cycle to work more often than women, although women travel shorter distances than men (Ortúzar et al., 2000; Dickinson et al., 2003; Vandenbulcke et al., 2009). Among other factors, women tend to give their personal security as a reason for not using a bicycle, and often make more complex trips than men due to family commitments (Pooley and Turnbull, 2000; Dickinson et al., 2003; Rietveld and Daniel, 2004; Gatersleben and Appleton, 2007).

Education also has a strong influence on bicycle use, but this depends on the area being studied. In North America a high educational level is positively associated with cycling (Noël, 2003; Plaut, 2005; Zahran et al., 2008), whereas the opposite effect is observed in Santiago (Chile) (Ortúzar et al., 2000) and Belgium (Hubert and Toint, 2002). Lastly, the professional field and status play a role (SSTC, 2001; Titheridge and Hall, 2006; Parkin et al., 2008; Heinen et al., 2009). For instance, Pucher et al. (1999) showed that in San Francisco lots of messengers are immersed in a cycling culture and use their bicycles in spite of the hilly topography. Bicycle use for commuting is generally high in academic towns (Martens, 2004; Rodríguez and Joo, 2004).

2.2. Cultural and societal determinants

The literature often mentions that societal and cultural factors influence bicycle use (see e.g. Jensen, 1999; Pucher et al., 1999; Ortúzar et al., 2000; Rietveld, 2001; Dickinson et al., 2003; Rietveld and Daniel, 2004; Plaut, 2005; Pucher and Buehler, 2006; Zahran et al., 2008). A low societal status often tends to be associated with commuter cycling, especially in countries where the car is dominant (e.g. US); utilitarian cycling is often considered as a fringe activity

and suffers from a renegade image (Pucher et al., 1999; Moudon et al., 2005). However, the cycling culture is quite developed in some Northern countries of Europe (e.g. the Netherlands, Sweden, Denmark, Germany and Belgium). Such differences between countries, regions or even ethnicities are probably explained by tradition and lifestyle. A meaningful example is provided by Rietveld and Daniel (2004), who show that immigrants with a different cultural background are unlikely to cycle in the Netherlands and prefer to use public transport or a car.

2.3. Environmental determinants

The main environmental determinants influencing bicycle use are relief, weather (and climatic conditions), urban spatial structure, and infrastructure. Hills influence the attractiveness of non-motorised modes of transport, and there is generally less cycling in hilly areas (Noël, 2003; Rodríguez and Joo, 2004). Cycling up hills is uncomfortable and requires substantial physical effort (Rietveld, 2001; Gatersleben and Appleton, 2007). It also affects travel time in the generalised cost function since it is slower than going down hill or on the flat.

Weather (short-term) and climatic (long-term) conditions are also often mentioned in the literature. Low or high temperatures (e.g. extreme heat combined with air pollution), frequent rain and strong winds may act as deterrents to commuter cycling (Nankervis, 1999; Richardson, 2000; Bergström and Magnusson, 2003; Parkin et al., 2008; Zahran et al., 2008; Koetse and Rietveld, 2009). Like topography, these factors decrease the level of comfort of cycling and increase the physical effort required.

The urban structure influences the likelihood of commuter cycling through several factors, such as population and job densities, mixed land-use and town size (Kitamura et al., 1997; Rietveld, 2001; Vandenbulcke et al., 2009). In urban areas, a high degree of connectivity (i.e. the ability to travel directly), associated with short distances (due to compactness and the presence of mixed-use activities) encourage cycling and walking in commuting trips (Saelens et al., 2003). Distance is an important barrier that limits cycling: only people living close to their workplaces will be interested in cycling (Kingham et al., 2001; Dickinson et al., 2003). Town size also seems to play a key role: few large cities (with more than 2 million inhabitants) have a bicycle commuting rate exceeding 10%. Medium-sized and compact cities perform better since they contain fewer barriers (e.g. motorways) and traffic densities are lower (Pucher et al., 1999). In the largest cities, proximity to the nearest stop and the high frequency of services also make public transport attractive and highly competitive for distances between 1 and 7.5 km. Up to 1 km, walking competes strongly with cycling (Pucher et al., 1999; Ortúzar et al., 2000; Witlox and Tindemans, 2004; Vandenbulcke et al., 2009).

Infrastructure (e.g. cycleways and cycle racks) is an essential ingredient for improving bicycle use and cyclists' safety (Hopkinson and Wardman, 1996; McClintock and Cleary, 1996; Rietveld, 2001). Well-planned and well-kept infrastructure (through design, maintenance and adequate connectivity) encourages cycling and reduces road accidents. Depending on the type of planning, several benefits can be provided for cyclists: e.g. improved comfort, reduced travel time, more enjoyment and increased safety. Dedicated paths (e.g. residential streets) as an alternative to main urban roads are an efficient way of reducing the exposure of cyclists to exhaust fumes (Hertel et al., 2008; Thai et al., 2008). Increased safety can also be achieved by developing continuous and designated cycle lanes, and ensuring that cyclists are still visible to motorists; this is often more highly valued by cyclists than other factors (e.g. reduced travel time, easy parking) (Hopkinson and Wardman, 1996; Tilahun et al., 2007). A well-developed network of cycleways combined with the provision of bicycle parking facilities at

stations/stops may improve the accessibility of public transport to cyclists (Bike-and-Ride), and hence, provide a competitive alternative to the car for commuting trips (Martens, 2004; 2007). Finally, the presence of facilities such as covered/secure cycle parking, lockers, showers and changing facilities at the workplace stimulates commuter cycling (Rietveld, 2000; Kingham et al., 2001; Dickinson et al., 2003; Pucher and Buehler, 2006; Van Malderen et al., 2009). Combined with the provision of continuous cycleways and a mileage allowance for cycling to work, such facilities are expected to have a significant impact on commuting by bicycle (Wardman et al., 2007; Van Malderen et al., 2009).

2.4. Policy-related determinants

Policy-related variables (i.e. planning and pro-cycling policies) play a key role in encouraging more and safer cycling through the implementation of a wide range of measures (Pucher et al., 1999; Rietveld, 2001; Dickinson et al., 2003; Pikora et al., 2003; Pucher and Buehler, 2008). Land-use planning can prevent urban sprawl by favouring compact and mixed-use solutions which reduce travelling distances and - consequently - favour the use of nonmotorised transport for commuting (Cervero and Kockelman, 1997; Kitamura et al., 1997; Meurs and Haaijer, 2001; Noël, 2003; Titheridge and Hall, 2006; Chapman, 2007; Woodcock et al., 2007). Moreover, transport planning can modify the design and lay-out of transport networks to improve the connectivity of bikeable roads between different destinations. It can increase the directness of travel through the creation of special intersection modifications for cyclists (e.g. priority signalling), the suppression of barriers (e.g. foot and cycle bridges over waterways and motorways), the creation of detours for car drivers, and the introduction of traffic-calming or car-free zones in urban centres (Meurs and Haaijer, 2001; Rietveld, 2001; Saelens et al., 2003; Pucher and Dijkstra, 2003; Pucher and Buehler, 2006; 2008). This makes cycling safer by reducing the risk of collision with motorised traffic, but also more convenient by allowing cyclists to avoid detours and traffic jams (Rietveld, 2001). Improving safety is of prime importance as it is well-known that the (perceived) risk of death and injury in traffic crashes strongly discourages people from cycling (Hopkinson and Wardman, 1996; McClintock and Cleary, 1996; Curtis and Headicar, 1997; Jacobsen, 2003; Pikora et al., 2003; Pucher and Dijkstra, 2003; Pucher and Buehler, 2006; Parkin et al., 2007). The provision of secure facilities (e.g. guarded cycle racks) along with police surveillance are also efficient means of reducing the risk of bicycle theft or vandalism (which are strong deterrents to cycling).

Financial measures can also promote non-motorised modes of transport and regulate the use of the private car. The provision of monetary incentives such as a mileage allowance or an employer-paid discount on the purchase of a new bicycle may stimulate the practise of commuting by bicycle (Kingham et al., 2001; van Wee and Nijland, 2007; Wardman et al., 2007). For instance, Wardman et al. (2007) showed that a payment of £2 per day could double the level of cycling in Great Britain. Higher parking fees, reduced space for car users (with increased 'shared space'), fiscal incentives for less polluting cars, higher fuel prices and the implementation of urban tolls (as in London and Stockholm) are some examples of push-measures which can decrease the attractiveness of private car use and encourage a shift to alternative modes of transport (Verhetsel, 1998; van Wee and Nijland, 2007).

Company-related factors can also encourage or discourage commuting by bicycle, especially through their organisational aspects (e.g. a strong dress code, the need to carry bulky goods), location policies, and the availability of facilities (e.g. changing rooms and cycle lockers at the workplace) (Curtis and Headicar, 1997; Dickinson et al., 2003; Heinen et al., 2009). In

particular, a remote location, far from any town or public transport, will result in great dependence on the car and will discourage employees from using any other mode of transport. Employees are also unlikely to travel to work by public transport or bicycle if their company provides free cars and fuel. Only reducing the provision of company cars and fuel, combined with other measures (e.g. incentives for cycling and public transport), can induce a shift away from the car towards alternative modes of transport (Kingham et al., 2001).

Finally, the promotion of cycling is important, since attitudes towards mobility, the environment, etc., are closely linked to travel behaviour (Kitamura et al., 1997). Such promotion can increase cycling and can be achieved through educational programmes (e.g. teaching cycling safety at schools), promotional events, the active involvement of advocacy groups and town officials (e.g. police officers on bicycles), and up-to-date information for cyclists (e.g. cycling maps showing 'bikeable' roads) (Curtis and Headicar, 1997; Pucher et al., 1999; Pucher and Buehler, 2006; Zahran et al., 2008). In particular, promotional events can create a mass effect providing cyclists with confidence and enthusiasm (Pucher et al., 1999). Linking cycling to health can also be an efficient way of encouraging more commuters to cycle, since regular exercise improves fitness and health (de Geus et al., 2008; 2009). Cycling is indeed a low-cost way to tackle health problems linked to physical inactivity (e.g. diabetes, cardio-vascular diseases and cancers). It has also been shown to improve mental health and productivity at work (Pucher et al., 1999; EC, 2000; van Wee and Nijland, 2007).

3. Spatial context

The empirical analyses conducted in this paper focus on Belgium, a small and highly urbanised country of more than 10 million inhabitants in a 30,000 km² area. Population densities range from 30 inhabitants/km² in rural regions to more than 20,000 inhabitants/km² in highly urbanised areas. With around 1.5 million inhabitants, Greater Brussels dominates the Belgian town network and is centrally located in the country. Urban sprawl nowadays threatens the quality of life in many Belgian cities. It is at the root of an increased dependence on the car, which causes a large number of negative externalities (congestion, pollution, etc.) (Dobruszkes and Marissal, 1994; Int Panis et al., 2001, 2004).

The popularity of cycling in Belgium is high on average, although far below the levels reported in the Netherlands and Denmark (Witlox and Tindemans, 2004). There has been a substantial decline in the use of bicycles since 1950, as the use of cars for routine trips has increased. The bicycle is now relegated to a marginal role, and is mainly used for recreational activities: indeed, in 2001, only 6.2% of commuters regularly used a bicycle as their main mode of transport (7.4% when bicycles were integrated into a multimodal chain). This compares to 68.6% of commuters who travelled by car (Verhetsel et al., 2007). However, in recent years there have been suggestions that a cycling renaissance is occurring in Belgium, as well as in a number of other European countries (Rietveld, 2001; Witlox and Tindemans, 2004). Furthermore, there are marked differences between Flanders (the northern, Dutch-speaking part of the country) on the one hand, and Wallonia and Brussels (the largely French-speaking southern and central parts) on the other hand. Some 91% of the commuter cyclists live in Flanders, whereas only 6.4% and 2.6% respectively live in Wallonia and Brussels. Several factors – such as cycling policies, culture and topography – are identified in Sections 6 and 7 of this paper to explain this difference.

4. Objectives and data

The main aim of this paper is to explain the variation of the proportion of commuters who travel by bicycle (dependent variable, y), as measured at the scale of the 589 municipalities in Belgium; note that y is continuous, non-negative and constrained to a specific range¹. Explanatory variables used in the multivariate analyses fall into three main categories (demographic and socio-economic, policy-related, and environmental) and refer to most of the determinants identified in Section 2. Appendix A lists and describes the explanatory variables. Note that the societal and cultural variables described in Section 2 were not included in this analysis, except through the integration of spatial regimes in the final model².

Most of the demographic and socio-economic variables come from the 2001 census (a self-administered questionnaire), carried out by the National Institute for Statistics (NIS, 2001b; NIS, 2004)³. The census provides data on individual and household features such as age, gender, level of education, presence of young children in the household, and subjective health which can be aggregated by municipality. Data related to income and car availability were also extracted from the NIS website.

Environmental and policy-related variables come from a wide range of sources. The variables selected for use in this paper not only result from policy decisions (e.g. land-use and transport-related measures), but also characterise the "environment" in which commuters live and travel. Some of these variables (such as population and job densities, average commuting distance, distance to the nearest town, town size, the percentage of commuters living within 10 km of their workplace, the percentages of urban/forest/agricultural land, and the percentage of the land dedicated to public/recreational services) are proxies for the urban structure, land use and accessibility of activities/facilities in the municipality. Others (such as the risk of accidents to cyclists, traffic volumes, the risk of bicycle theft, dissatisfaction with cycling facilities, hilliness, and air pollution) are representative of the overall convenience of cycling in the municipality.

5. Methodology

A combination of exploratory (spatial) data analyses and spatial econometric techniques was employed, using several statistical software packages (SAS, GeoDa and R). Descriptive statistics and bivariate analyses were computed first, to explore the relationships between each of the explanatory variables and the dependent variable y (i.e. the proportion of commuting which is by bicycle). Multivariate models were then applied, with the aim of examining the relative importance of the explanatory variables for the spatial variation in bicycle use (at the scale of municipalities). To improve the statistical inference process, special attention was paid to multicollinearity, spatial heterogeneity (i.e. heteroskedasticity and/or structural instability) and spatial autocorrelation.

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¹ Linear models could be hence less suited here; however, good results are obtained and suggest that the methodological approach adopted here is quite satisfactory.

² Exploratory spatial data analyses (ESDA) does indeed suggest that the regimes/clusters defined in Section 5 are representative of different cultures (the Flemish-Walloon split).

³ The census is preferred to other surveys (e.g. NIS, 2001a) since it is the most recent database and covers the entire population.

5.1. The validity of the ordinary least squares model

The first step in testing the validity of the ordinary least squares (OLS) model was to compute condition indices, tolerance and variance inflation factor (VIF) values so as to diagnose the existence of multicollinearity. The major assumptions of the regression (linearity, homoscedasticity, normality and spatial independence of the residuals) were then tested. The White, Breusch-Pagan and Koenker-Bassett tests for the presence of heteroskedasticity were performed first, and the asymptotic version HC3 of the heteroskedasticity-consistent covariance matrix (HCCM) was then used to correct for heteroskedasticity (Long and Ervin, 2000). Lagrange multiplier (LM) diagnostics and their robust forms (Robust *LM*) were preferred to Moran's *I*, because they help to identify the form of spatial dependence (spatial error or spatial lag) and because Moran's *I* is inappropriate in the presence of heteroskedastic or non-normally distributed errors (Anselin and Rey, 1991; Anselin and Florax, 1995; Anselin et al., 1996; Anselin, 2005). Finally, the Jarque-Bera statistic was used to test the assumption of normality.

5.2. Spatial autoregressive modelling

Spatial autoregressive modelling (SAR) was used to deal with the presence of spatial autocorrelation. It is divided into two alternative specifications: spatial error and spatial lag models. While the first specification suggests the presence of omitted explanatory variables, the second indicates the possibility of a diffusion process (i.e. an event in one municipality increases the likelihood of the same event occurring in neighbouring municipalities).

The spatial error model (SEM) specifies a spatial autoregressive process for the error term ε to account for the spatial influence of unmeasured (or omitted) explanatory variables on the proportion of commuting by bicycle in neighbouring municipalities. For N observations and K exogenous independent variables, the structure of the SEM in matrix form is:

$$y = X\beta + \varepsilon \tag{1}$$

with
$$\varepsilon = \lambda W \varepsilon + \xi$$
 (2)

where y is a $N \times 1$ vector of observations i of the dependent variable (proportion of commuting by bicycle in municipality i), β is a $K \times 1$ vector of coefficients of the independent variables, X is a $N \times K$ matrix of observations i of the independent variables (including a constant term), ε is a $N \times 1$ vector of error terms at location i, λ is a spatial autoregressive coefficient, W is a $N \times N$ spatial weights matrix (row-standardised) and ξ is a white noise error. In this study, N = 589 (the number of municipalities in Belgium).

By contrast, the spatial lag model (SLM) assumes that the dependent variable in municipality i is influenced by the values of the dependent and independent variables in the surrounding municipalities j. The magnitude of this spatial influence (or "spillover effect") is captured by a spatial autoregressive coefficient ρ . In matrix notation, the SLM specification is:

$$y = \rho W y + X \beta + \varepsilon \tag{3}$$

where Wy is the spatially lagged endogenous variable.

Note that for both specifications (lag and error), the standard R^2 is invalid since a maximum likelihood (ML) estimation is used. Some more appropriate measures of fit are the log-

likelihood, the Akaike information criterion (AIC) and the Schwarz information criterion (SIC) (Anselin, 1988; Anselin, 2005). The validity of the White and Breusch-Pagan tests is also strongly affected when the error terms are spatially correlated (Anselin, 1988). Two alternative tests are hence preferred: the joint LM test and the spatial Breusch-Pagan test. Further details are provided by Anselin (1988), Anselin and Griffith (1988), Le Gallo (2004) and Bivand (2008) about these tests.

5.3. Spatial heterogeneity

Spatial heterogeneity was taken into account in a number of ways. These include focusing on the issue of heteroskedasticity (see Sections 5.1 and 5.2), and testing for the structural stability of coefficients between spatial subsets of the data (spatial regimes). In the presence of structural instability, the parameter estimates take on different values in distinct geographic areas. Formally, a regression with Regimes 1 and 2 (e.g. north and south) is called a spatial regime regression and is expressed as:

$$\begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} X_1 & 0 \\ 0 & X_2 \end{bmatrix} \begin{bmatrix} \beta_1 \\ \beta_2 \end{bmatrix} + \begin{bmatrix} \varepsilon_1 \\ \varepsilon_2 \end{bmatrix}$$
 (4)

where y_1 and y_2 are the vectors of observations of the dependent variable, β_1 and β_2 are the vectors of coefficients of the independent variables, X_1 and X_2 are the matrices of observations of the independent variables (including a constant term for each regime), and ε_1 and ε_2 are the vectors of error terms for Regimes 1 and 2 respectively.

If spatial dependence persists after the spatial heterogeneity has been modelled, the spatial regime specification (4) should also account for spatial autocorrelation. Equation (3) hence takes on the form:

Regime 1:
$$y_1 = \rho W_1 y_1 + X_1 \beta_1 + \varepsilon_1$$
 (5)
Regime 2: $y_2 = \rho W_2 y_2 + X_2 \beta_2 + \varepsilon_2$ (6)

Regime 2:
$$y_2 = \rho W_2 y_2 + X_2 \beta_2 + \varepsilon_2$$
 (6)

where W_1 and W_2 are the spatial weights matrices for Regimes 1 and 2 (Le Gallo, 2004; Anselin, 2007; Bivand, 2008).

5.4. Diagnostics for structural instability

The stability of the coefficients across regimes can be diagnosed using the spatially adjusted version of the Chow test, i.e. the spatial Chow test (C_G) (Anselin, 1988). It can also be detected and visualised using an exploratory spatial data analysis (ESDA). This helps to identify the presence of global and local patterns of spatial autocorrelation and heterogeneity (e.g. spatial outliers or clusters) in the proportion of commuting by bicycle (Anselin, 1998a; 1998b; Le Gallo and Ertur, 2003; Baller et al., 2001; Ramajo et al., 2008). ESDA can be undertaken by performing common measures of spatial autocorrelation, such as the Moran's I statistic, the Moran scatterplot and the local indicators of spatial association (LISA) (Anselin, 1995; Le Gallo, 2004).

In particular, the Moran scatterplot allows the local spatial association (between a municipality and its neighbours) to be categorised into four groups: HH (municipality with a high value surrounded by municipalities with high values), LH (low value surrounded by high values), LL (low value surrounded by low values) and HL (high value surrounded by low

values). HH and LL refer to spatial clusters (positive spatial autocorrelation), while LH and HL indicate to spatial outliers (negative spatial autocorrelation). Finally, the information derived from the categorisation into four groups, combined with that resulting from the computation of the significance values of LISA yields the LISA cluster map. This gives an indication of the location of significant spatial clustering and diagnoses local instability (e.g. pockets of non-stationarity). It hence facilitates the identification of spatial outliers and spatial regimes (Le Gallo and Ertur, 2003; Baller et al., 2001).

6. Results

6.1. Basic statistics and bivariate correlations

Appendix B presents some basic statistics and shows that most of the explanatory variables are significantly correlated with the dependent variable (with the expected signs). The highest correlations are observed for the variables measuring dissatisfaction with cycling facilities (-0.82), slope (-0.77), bad health (-0.58), young workers (0.54) and long commuting distances (-0.54). Other variables which are negatively correlated with commuting by bicycle are the proportion of working households with young children (-0.39), middle-aged workers (-0.39), forests (-0.33) and the risk of accidents to cyclists (-0.32). Conversely, the density of jobs (0.38), urbanisation (0.34), and traffic volume on regional roads (0.31) all have positive spatial correlations with cycle commuting. Most of these relationships confirm the hypotheses about transport-choice processes set out in Section 2. The positive correlation with traffic volumes is the only anomaly, which is probably explained by the high proportion of cyclists in urbanised areas (where traffic congestion is also high).

6.2. Diagnostics (OLS)

A multivariate regression was first applied using OLS estimation and paying special attention to the heteroskedasticity and multicollinearity issues. The analysis of condition indices, tolerance and VIF values is helpful to lower multicollinearity as much as possible. The Breusch-Pagan and White tests for heteroskedasticity (Table 1) reveal the presence of nonconstant error variance in the model; this was corrected using White's correction (HC3). Results for the White-corrected OLS estimation are reported in Table 2, and indicate quite high goodness-of-fit ($R^2 = 0.879$). Most of the parameters are significant at least the 10% level of probability.

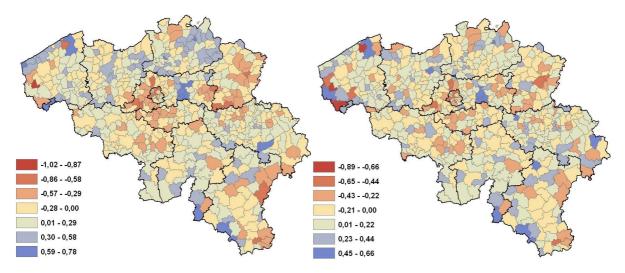
The diagnostics in Table 1 (Moran's *I*, LM and joint LM tests) do, however, show the presence of spatial dependence, which affects the validity of the OLS estimations. The analysis of the significance of the robust and non-robust forms of the LM tests indicates that the spatial lag model is a better way of addressing the spatial autocorrelation issue.

6.3. Choice of the spatial weight matrix

The computation of a spatial autoregressive model requires the definition of a spatial weight matrix. Here, a "queen" contiguity-based matrix (first order of contiguity; row-standardised) is used because it provides the best fit and results in a model satisfying to the finite sample condition (Wald test \geq likelihood ratio \geq Lagrange multiplier) (Anselin, 1988). In the queen case, the elements w_{ij} of the weights matrix W are equal to 1 when the municipalities have common borders and/or vertices (0 otherwise).

6.4. Spatial lag results

The results for the spatial lag models are presented in Table 2. White's correction is again used to treat the model for the presence of heteroskedasticity. As the significant Jarque-Bera statistic in Table 1 suggests, the ML estimation is valid since the error terms are normally distributed. The same is true for the LM tests and Moran's *I* statistics. The spatial lag model gives a better fit than OLS: the log likelihood statistic increases from -102.4 to 33.7 (Table 2). Moreover, the Moran's *I* and the LM test statistics both indicate that including a spatially lagged variable in the model eliminates spatial dependence. This is confirmed by Figures 1a and 1b, which show the spatial autocorrelation of errors to be substantially less in the ML estimation than in the OLS model. This reduction translates into fewer spatial concentrations of similar residuals. The example of Brussels and its periphery is a good example of this: similar OLS residuals are spatially concentrated (Figure 1a), but the ML residuals (Figure 1b) are much less so.



Figures 1a and 1b: OLS (left) and ML residuals (right). The Brussels-Capital Region is centrally located on these maps (see Figure 2). Moran's I = 0.34 and is significant.

Table 2 shows that the spatial autoregressive coefficient ρ (or lag coefficient) is highly significant. This is suggestive of the fact that spillover influences exist between one municipality i and its neighbourhood: the likelihood of cycling in i is (positively) linked to bicycle use in the neighbouring municipalities j. The significance and magnitude of all the regression coefficients are lower for the ML estimation than for OLS, which can be explained by the introduction of ρ . This suggests that part of the explanatory power of variables in municipality i may really be due to the influence of the neighbouring municipalities j (which is picked up by ρ). Among the significant coefficients, the average change in relative value is high (47%) and illustrates the substantial bias of the OLS model coefficients when spatial dependence is ignored.

| | OLS | ML |
|---------------------------------------|----------|----------|
| Diagnostics for normality | | |
| Jarque-Bera test | 4,62 | - |
| Diagnostics for multicollinearity | | |
| Variance Inflation Value (max. value) | 3,30 | - |
| Condition index (intercept adjusted) | 5,03 | - |
| Diagnostics for heteroskedasticity | | |
| Breusch-Pagan test ¹ | 31,33*** | 36,87*** |

| Koenker-Bassett test ² | 28,32** | 28,82*** |
|--|-----------|-----------|
| White test | 213,64*** | - |
| Breusch-Pagan test (North-South) ³ | 88,68*** | 25,08*** |
| Diagnostics for spatial dependence | | |
| Moran's I of residuals ⁴ | 0,34*** | 0,01 |
| Lagrange Multiplier (lag) | 253,37*** | - |
| Robust LM (lag) | 86,74*** | - |
| Lagrange Multiplier (error) | 181,96*** | - |
| Robust LM (error) | 15,33*** | - |
| Diagnostic for spatial dep. and heteroskedasticity | | |
| Joint test LM | 213,29*** | - |
| Tests on overall stability | | |
| Chow structural instability test ⁵ | 14,20*** | 120,49*** |
| Diagnostics for residual autocorrelation | | |
| LM test | - | 0,00 |

^{*}Significant at the 90% level

Table 1: Regression diagnostics for the OLS and ML estimations

| | OLS, with heterosk. correction | ML, with heterosk. correction |
|--|-----------------------------------|----------------------------------|
| Intercept | 6,4124*** | 3,2698*** |
| | [0,0000] | [0,0000] |
| Lag coefficient (<i>ρ</i>) | - | 0,6015*** |
| | - | [0,5483] |
| Demographic variables | | |
| Working men | 0,0472*** | 0,01673** |
| | [0,1150] | [0,0408] |
| Age 2 (45-54 years) | -0,0460*** | -0,02505*** |
| | [-0,1352] | [-0,0737] |
| Age 3 (> 54 years) | -0,2054* | -0,14503* |
| | [-0,0456] | [-0,0322] |
| Young children | -0,0567*** | -0,0218*** |
| | [-0,1865] | [-0,0716] |
| Socio-economic variables | | |
| Education 3 (higher/university degree) | -0,4988*** | -0,23034*** |
| | [-0,1261] | [-0,0582] |
| Income | 0,0030 | 0,00852 |
| | [0,0072] | [0,0206] |
| Bad health | -0,0521*** | -0,0189*** |
| | [-0,3124] | [-0,1133] |
| Environmental and policy-related variables | | |
| Commuting distance | -0,0114*** | -0,00652** |
| | [-0,0789] | [-0,0450] |
| City size | -0,0954*** | -0,0875*** |
| | [-0,1750] | [-0,1604] |
| Traffic volume 2 (municipal network) | -0,9216*** | -0,4695*** |

^{**}Significant at the 95% level

^{***}Significant at the 99% level

n.a.: no test available

¹ The spatial Breusch-Pagan test was used for the ML estimation
² The spatial Koenker-Bassett test was used for the ML estimation
³ Inference computation based on 9999 permutations (for ML estimation only)
⁴ The spatial Chow structural instability test was used for the ML estimation

| | [-0,1341] | [-0,0683] |
|-------------------------------------|------------|-------------|
| Slopes | -0,4873*** | -0,1763*** |
| | [-0,2655] | [-0,0961] |
| Cycling facilities unsatisfaction | -0,0127*** | -0,0049*** |
| | [-0,2818] | [-0,1077] |
| Accident risk | -0,1673** | -0,14495*** |
| | [-0,0500] | [-0,0434] |
| Air pollution | 0,0141*** | 0,00405 |
| | [0,0717] | [0,0206] |
| N | 589 | 589 |
| R-squared (<i>R</i> ²) | 0,879 | - |
| Ajusted R-squared | 0,876 | - |
| F-value | 297,80*** | - |
| Log Likelihood | -102,43 | 33,68 |
| Akaike information criterion (AIC) | 236,86 | -35,36 |
| Schwarz information criterion (SIC) | 306,91 | 34,70 |

^{*}Significant at the 90% level

Standardized regression coefficients in brackets *Italic*: variables logarithmically transformed

Table 2: Regression coefficients for the OLS and ML estimations

The signs of the regression coefficients in Table 2 are the same for the OLS and ML estimations. As expected, most of the (significant) explanatory variables introduced in the models have a deterrent effect on the proportion of commuters cycling. Municipalities with high proportions of working people over 45, working households with one or more young children, or inhabitants in poor health have lower levels of commuter cycling. Municipalities characterised by large numbers of highly-educated people also have lower levels of commuter cycling, which confirms the results of previous studies in Belgium (SSTC, 2001; Hubert and Toint, 2002). On the other hand, high levels of cycling are observed in municipalities with high proportions of working men. Among the environmental and policy-related variables, the presence of high accident risks, heavy traffic volumes and steep slopes along the road network are associated with a low propensity to cycle to work. The size of the town also matters, and this is probably associated with the provision of good facilities for cycling. The proportion of commuters cycling is highest in the cities (well-equipped municipalities), and lowest in small municipalities (Vandenbulcke et al., 2009).

Note finally that, when the regression is carried out on the proportion of cyclists among commuters who travel less than 10 km (in municipality *i*), the results (not shown here) are basically similar to those shown in Table 2. The main difference lies in the variable referring to commuting distances: for commuting trips of up to 10 km, increasing distance is linked to more cycling, whereas in the general regression (Table 2) increasing distance is linked to less cycling. Cycling is a very convenient mode of transport for distances between 2 and 5 km, but for shorter distances (0–2 km) walking is the preferred mode of transport (Vandenbulcke et al., 2009). This suggests that, up to 10 km, commuting distance does not act as a strong deterrent to cycling. Given that approximately 39% of commuters (and even more in urban areas) live less than 10 km from their work, there is considerable potential for a shift to cycling.

^{**}Significant at the 95% level

^{***}Significant at the 99% level

^{- :} variable not included in the model

6.5. Accounting for spatial heterogeneity

6.5.1. Diagnostics: Chow tests and exploratory spatial data analyses (ESDA)

Structural instability is detected by the Chow test and its spatial extension. Both tests are highly significant and hence clearly reject the null hypothesis of parameter stability. This suggests that the spatial lag results (Table 1) do not completely account for spatial heterogeneity. ESDA techniques confirm these findings and help to identify spatial regimes. The global spatial autocorrelation for the proportion of commuters cycling was first tested using the Moran's I statistic. This indicated the presence of a positive and significant spatial autocorrelation (I = 0.90; p = 0.0001), which means that municipalities with high rates of cycle commuting are generally located close to other municipalities with high rates (and similarly municipalities with low rates are located close to other municipalities with low rates).

The Moran scatterplot and the LISA cluster map for the dependent variable in Figure 2 help us to identify spatial regimes. The results of the Moran scatterplot suggest the presence of spatial heterogeneity in the form of two distinct spatial regimes, in quadrants I and III. The LISA cluster map illustrates the spatial pattern of these regimes and reveals a clear-cut north/south division of the municipalities: most of the northern municipalities (Flanders) fall into quadrant I, while a large proportion of the southern municipalities (Wallonia and Brussels) fall into quadrant III.

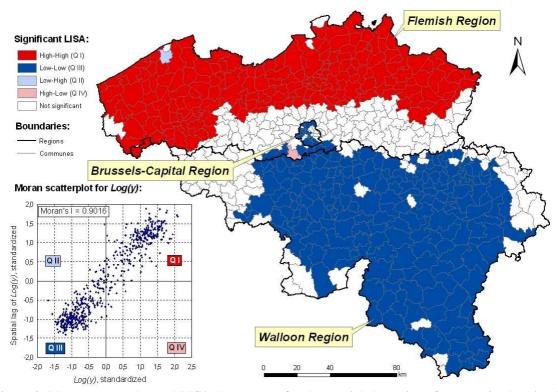


Figure 2: Moran scatterplot and LISA cluster map for the spatial clustering of commuting by bicycle

6.5.2. Spatial regime regression with a spatially lagged variable

The northern and southern spatial regimes were incorporated into the regression to adjust for spatial heterogeneity. The diagnostics in Table 3 show the existence of spatial autocorrelation and heteroskedasticity in the models. This was corrected by applying an ML estimation (lag)

and a White's correction (Table 4). The spatial regime specification (with spatial lag) gives a considerably better fit than the spatial lag model, with a log likelihood statistic as high as 93.9 (Table 4).

| | OLS, with spatial regimes | ML, with spatial regimes |
|---|---------------------------|--------------------------|
| Diagnostics for heteroskedasticity | | |
| Breusch-Pagan test ¹ | 112,44*** | 94,46*** |
| Koenker-Bassett test ² | 93,64*** | 79,74*** |
| Diagnostics for spatial dependence | | |
| Moran's / of residuals ³ | 0,29*** | -0,20 |
| Lagrange Multiplier (lag) | 200,25*** | - |
| Robust LM (lag) | 76,96*** | - |
| Lagrange Multiplier (error) | 130,33*** | - |
| Robust LM (error) | 7,04*** | - |
| Diagnostic for spatial dep. and heterosk. | | |
| Joint LM test | 242,77*** | - |
| Diagnostics for residual autocorrelation | | |
| LM test | - | 0,16 |

^{*}Significant at the 90% level

Table 3: Regression diagnostics for the OLS and ML estimations, including the spatial regimes

The results in Table 4 show that several explanatory variables are significant for the north (Flanders) but not for the south (Wallonia and Brussels), and vice versa. The signs of the significant coefficients are the same as in the spatial lag specification, but the magnitude differs greatly in some cases. For Flanders, the average change in the (relative) values ranges from 6.4% for dissatisfaction with cycling facilities to 426.5% for the accident risk. For Wallonia and Brussels, this change is less pronounced, ranging from 2.7% for the risk of an accident, to 58.7% for town size. These findings not only illustrate how biased the estimates are when the structural instability is ignored, they also show the substantial difference in the size of these estimates between the Belgian regions. The "accident risk" variable is probably the best example of this.

| | ML, with spatial regimes and | heteroskedasticity co |
|----------------------|------------------------------|-----------------------|
| | North | South |
| Intercept | 2,3084* | 4,3095*** |
| | [0,000] | [0,0000] |
| Lag coefficient (ρ) | 0,53 | 62*** |
| | [0,5 | 097] |
| emographic variables | | |
| Working men | 0,0296** | 0,0008 |
| | [1,0246] | [0,0288] |
| Age 2 (45-54 years) | -0,0417** | -0,0205*** |
| | [-0,5854] | [-0,3007] |
| Age 3 (> 54 years) | -0,1074 | -0,0680 |
| | [-0,1317] | [-0,0867] |

^{**}Significant at the 95% level

^{***}Significant at the 99% level

^{- :} no test available

¹ The Spatial Breusch-Pagan test is used for the ML estimation

² The Spatial Koenker-Bassett test is used for the ML estimation

³ Inference computation based on 9999 permutations (for ML estimation only)

| Young children | -0,0365*** | -0,0247*** | |
|--|---|------------|--|
| | [-0,4372] | [-0,3306] | |
| Socio-economic variables | | | |
| Education 3 (higher/university degree) | -0,0968 | -0,3132*** | |
| | [-0,2104] | [-0,6862] | |
| Income | 0,0311* | -0,0027 | |
| | [0,3824] | [-0,0307] | |
| Bad health | -0,0098 | -0,0146** | |
| | [-0,1274] | [-0,2481] | |
| Environmental and policy-related variables | | | |
| Commuting distance | -0,0165*** | -0,0047* | |
| | [-0,2061] | [-0,0765] | |
| City size | -0,1146*** | -0,0361*** | |
| | [-0,4539] | [-0,1483] | |
| Slopes | -0,1931** | -0,1972*** | |
| | [-0,1145] | [-0,1966] | |
| Cycling facilities unsatisfaction | -0,0052*** | -0,0045*** | |
| | [-0,1666] | [-0,2227] | |
| Accident risk | -0,7632*** | -0,1489*** | |
| | [-0,1047] | [-0,0493] | |
| Air pollution | 0,0138*** | -0,0054 | |
| | [0,2551] | [-0,0956] | |
| Traffic volume 2 (municipal network) | -0,2357 | -0,4521** | |
| | [-0,0306] | [-0,0700] | |
| N | 589 ($N_{North} = 308$; $N_{South} = 281$) | | |
| Log Likelihood | 93,9 | 923 | |
| Akaike information criterion (AIC) | -123 | ,846 | |
| Schwarz information criterion (<i>SIC</i>) | 16,264 | | |

^{*}Significant at the 90% level

Standardized regression coefficients in brackets *Italic*: variables logarithmically transformed

Table 4: Regression coefficients for the spatial regime specification (ML estimation)

6.5.3. Regional variation and the relative importance of the variables

Table 4 suggests that variables such as median income and the proportion of working men are not significantly related to the rate of cycle commuting in Wallonia and Brussels; on the other hand, they are positively related to the rate in Flanders. The positive association between median income and bicycle use can probably be explained by the fact that lower median income is a proxy for crime and vandalism (Parkin et al., 2008). This suggestion is supported by a significant correlation of -0.20 between the median income and the number of bicycle thefts in a municipality (and a correlation of -0.27 between median income and the risk of bicycle theft). The relationship between cycle commuting and the air pollution (the annual mean concentration of PM10s) was also only significant in Flanders. Surprisingly, Figure 3 shows that, on its own, an increase in the PM10 concentration actually increase the rate of cycle commuting in a Flemish municipality: for instance, an increase from 25 to 30 μ g/m³ is linked to an increase in the proportion of commuting by bicycle of 8.1%. This is probably explained by the fact that the health risks of air pollutants are not really perceived as barriers to cycling (since cycling is seen as beneficial for health, despite the increased exposure).

^{**}Significant at the 95% level

^{***}Significant at the 99% level

Moreover, it suggests that commuter cycling is more common in industrial and/or congested urban environments (which are generally areas with high concentrations of PM10s).

Table 4 shows that three variables which are not significantly related to bicycle use in Flanders do appear to have an impact in Wallonia and Brussels (the southern part of Belgium). The results suggest that a one percentage point decrease in the proportion of inhabitants reporting bad health will increase bicycle use by 0.07%. Relatively good physical and mental health is indeed required to use a bicycle. Moreover, a decrease from 25 to 15% in the proportion of highly qualified people in a municipality is linked to a 17.8% increase in commuter cycling⁴. Commuters with better qualifications generally get higher wages and fringe benefits such as a company car; this probably explains why they are more likely to have a car at their disposal, and so choose to live far from their workplace, beyond "cycling distance". Finally, a reduction in the volume of motorised traffic is expected to encourage cycling: a decrease from 200,000 to 100,000 vehicle-km per kilometre of local road per year is predicted to increase bicycle use by 5.23% (Figure 4). Concretely, such a reduction corresponds to a 1,700-km decrease in the mileage of motorised vehicles per municipality per year, or a 4.6-km decrease in the daily mileage⁵. Ideally, a substantial reduction in traffic, from 1,000,000 to 10,000 vehicle-km (achieved, for example, through the implementation of an urban toll in the municipality) could increase bicycle use by as much as 32%.

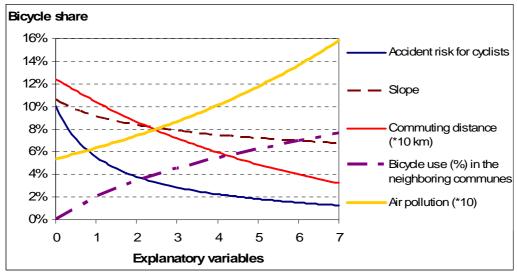


Figure 3: Variation in bicycle use in Flanders as explanatory variables change. Note: these graphs are constructed by varying one explanatory variable, while holding all the others constant at their means (see Rodríguez and Joo, 2004). For ease of illustration, all the explanatory variables are all presented on the same x-axis. Given that the validity of the results may be affected by the presence of feedback effects in the model (LeSage and Fisher, 2008; LeSage and Pace, 2009), we compared the parameter estimates in Table 4 with scalar summary impact measures and observed that feedback effects are quite weak. As a result, the parameter estimates give a reasonable measure of the direct impact of changes (in explanatory variables) on cycling levels in *i*.

⁴ Note that this result holds for Wallonia, but does not really applies to Brussels, where most commuter cyclists (66%) are highly qualified. Such a result is explained by the greatest weight of the Walloon municipalities (262 municipalities, compared with the 19 Brussels municipalities).

⁵ Assuming a 169-km local road network and 10,000 motorised vehicles using this network each year. These figures are based on the averages for Belgian municipalities.

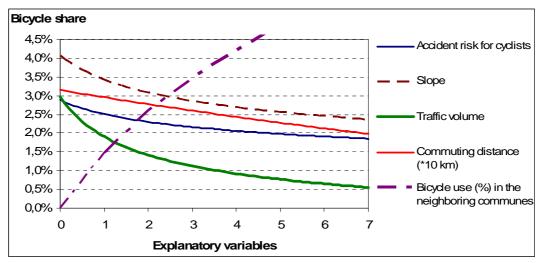


Figure 4: Variation in bicycle use in Wallonia and Brussels as explanatory variables change. Note: these graphs are constructed by varying one explanatory variable, while holding all the others constant at their means (see Rodríguez and Joo, 2004). For ease of illustration, all the explanatory variables are all presented on the same x-axis. Given that the validity of the results may be affected by the presence of feedback effects in the model (LeSage and Fisher, 2008; LeSage and Pace, 2009), we compared the parameter estimates in Table 4 with scalar summary impact measures and observed that feedback effects are quite weak. As a result, the parameter estimates give a reasonable measure of the direct impact of changes (in explanatory variables) on cycling levels in *i*.

Most of the other explanatory variables shown in Table 4 have significant relationships with bicycle use in both regions. At first glance, variables such as the proportion of households with young children, or the proportion of commuters aged 45 to 54, seem to be strong deterrent factors for cycling. Their impact is also pronounced in Flanders, than in Wallonia and Brussels. Combined with the results of a principal component analysis (orthogonal varimax rotation; results not reported here), these findings also suggest that: (1) being young (i.e. less than 25 years of age) and having poor qualifications increases the propensity to cycle to work; (2) having more than one young child in the household increases the probability of owning a car, and consequently decreases the likelihood of cycling.

Table 4 also shows the impact town size and dissatisfaction with cycling facilities have on cycle commuting. In both regions, a 10% increase in the proportion of household which express dissatisfaction with the facilities for cycling would reduce bicycle use by about 5.5%. Living in a poorly-equipped municipality (in terms of facilities) is associated with a lower likelihood of using a bicycle, whereas larger towns have a higher proportion of cycle commuting. In Flanders, the largest cities (H_1 to H_3) score well with cycle commuting rates 31.3 to 58.5% higher than in the most rural municipalities (H_6 to H_8). In Wallonia and Brussels, this difference is less pronounced, and only ranges from 3.4 to 9.7%.

Last but not least, Figures 3 and 4 suggest that a high risk of accidents, long commuting distances and hilly terrain decrease the propensity to cycle. Although it is basically similar in the two regions, the impact of the topography on bicycle use is slightly greater in the southern part of the country. An increase of the mean slope of the road network from 1 to 2° (which might occur, for example, when commuters are forced to take an alternative route, due to roadworks or deviations) could reduce the number of commuting cyclists by more than 8.4% in Flanders and 9.9% in Wallonia and Brussels. Conversely, reducing the slopes would significantly increase bicycle use, especially in municipalities where the mean slope is 1 to 2°. Above this "limit", the impact of a change in the mean slope is lower. The risk of accidents

also strongly discourage bicycle use. In Flanders, an increase in this risk from 0.0 to 0.5 (which corresponds to two more victims per year and per 100,000 bicycle-minutes) is linked to a 29.3% reduction in the number of commuter cyclists. In Wallonia and Brussels, the accident risks is also negatively linked to bicycle use, but to a lesser extent: the same increase in risk (from 0.0 to 0.5) is linked to a fall in bicycle use of only 7.9%. Longer commuting distances have a deterrent effect and do not stimulate cycling. In Flanders, an increase in the average commuting distance from 5 to 15 km would produce a 16.6% decrease in commuter cycling. The same increase in commuting distance in Wallonia and Brussels would reduce the bicycle use by 6.1%. Given that the "commuting distance" variable partly synthesises proximity-related information (through variables such as population and job densities, and urbanised areas)⁶, it implies that compact environments and tight town networks are associated with low commuting distances and hence stimulate cycling.

6.5.4. Spatially lagged variable

Table 4 shows that the coefficient ρ is still highly significant and positive for the spatial regime model. This indicates the presence of a strong diffusion process between neighbouring municipalities: the (neighbouring) municipalities j exert a positive spillover effect on the propensity to cycle in municipality i, which in turn (after t years) could generate a feedback effect on bicycle use in j. In the long-term, such a continuous diffusion process could initiate a "mass effect", in the form of a virtuous circle which maintains the propensity to use a bicycle for commuting in the region. The municipalities in Wallonia and Brussels seem to be prone to a large reduction in bicycle use if cycling becomes less popular in neighbouring municipalities (and conversely), but Flemish municipalities are more resistant (relatively to Wallonia and Brussels) to the possibility of a fall in bicycle use in surrounding municipalities.

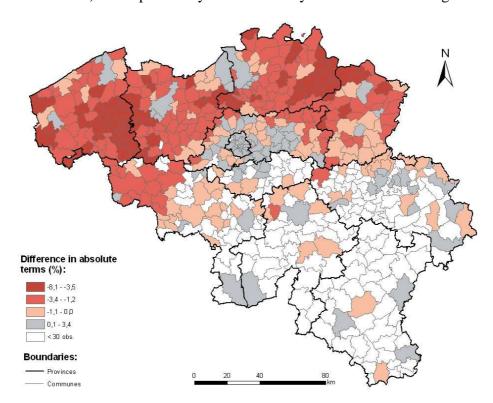


Figure 5: Percentage changes (in absolute values) in cycle commuting between 1991 and 2001 Source: Verhetsel et al. (2007)

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⁶ This result is supported by the findings of the principal component analysis (not reported here).

As suggested by Figures 3 and 4, the spillover effect is most pronounced when municipality i and its neighbouring municipalities j all have low rates of cycle commuting: for instance, when the spatially lagged variable Wy is lower than 5%, bicycle use in municipality i still increases but to a lesser extent. Such diffusion processes can be observed in reality, which reinforces the validity of the model. Figure 5 shows that the changes in bicycle use in Belgium between 1991 and 2001 were spatially clustered. For instance, there was an increase in bicycle use in Brussels and its neighbourhood during this period, but the opposite was true in several groups of municipalities in the western and north-eastern parts of the country.

6.5.5. Analysis of the residuals

The residuals of the final specification (Table 4) are mapped in Figure 6. This provides a useful tool for planners and policy makers since it pinpoints both the municipalities that 'over-perform' in terms of bicycle use and those where there is still potential to develop the use of the bicycle for commuting trips further. This potential exists in the municipalities characterised by negative residuals (predicted values > observed values). Given the current environment and neighbourhood⁷, such municipalities could perform better in terms of bicycle use but, for something (e.g. an inadequate or unambitious cycling policy, high-quality public transport, a multicultural town⁸) holds it back. Examples of municipalities with negative residuals are Antwerp, Brussels, Genk, Ghent and Kortrijk (Courtrai). The last two are surprising, in view of their pro-cycling policies and relatively high rates of cycle commuters, but suggest that there is still potential to encourage more people to cycle to work.

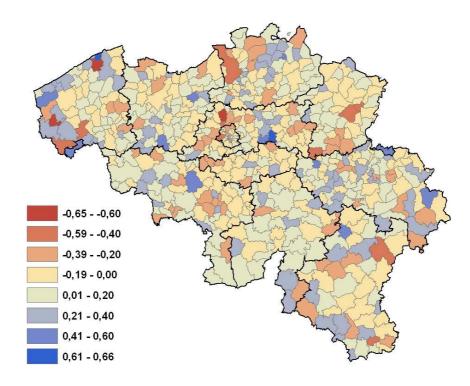


Figure 6: The residuals of the spatial regime specification (see Table 4)

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⁷ The "neighbourhood" here refers to the region (Flanders or Wallonia and Brussels) in which municipality i is located, and the rate of cycling in the neighbouring municipalities j.

⁸ Immigrants and inhabitants with a foreign background have different cultural reference points, and are generally less likely to cycle (public transport and/or the car are preferred to the bicycle) (Rietveld and Daniel, 2004). In municipalities with a high proportion of foreigners (e.g. Ghent, Brussels, Antwerp), bicycle use is generally lower than in other municipalities with the same environmental features.

At the other end of the scale, positive values of the residuals mean that the observed rate of commuter cycling is higher than predicted by the model. Municipalities characterised by positive values excel in terms of bicycle use (given their environment). The examples of Louvain and Bruges are important in this respect, since they have more pro-cycling policies (in terms of engineering, traffic education and enforcement) than other Flemish municipalities. Several municipalities in Wallonia (e.g. Mouscron, Perwez, Hotton) also perform better than expected, despite their low absolute rates of cycle commuting. Given their environment (steep slopes, rural setting, etc.), they "over-perform", for example by adopting mobility strategies that encourage bicycle use (SPW, 2008).

7. Discussion and re-cycling strategies

7.1. Socio-economic variables: education, promotion and training

Income, age and gender all have a significant impact on the rate of cycle commuting in Flanders: low median income, low proportions of working women, and a young (under 45) workforce are all associated with high rates of cycling to work. Having one or more young children (0–5 years old) in the household decreases the likelihood of cycling to work in both regions. The presence of many highly-qualified people also matters, particularly in the province of Walloon Brabant. Highly qualified commuters living in Wallonia generally have high incomes, can afford a car, and use it to travel large distances⁹. They are hence less likely to use a bicycle for their commuting trips (Jensen, 1999).

Promotional and educational campaigns (focused on, for example, health benefits or the possibilities of bike pooling¹⁰) could be helpful in addressing some of these socio-economic issues (Pucher and Dijkstra, 2003). Public and private companies should promote existing alternatives to the car, and try to make them competitive by providing financial incentives such as a mileage allowance or a company bicycle.

7.2. Environmental variables: towards optimal paths?

Flat terrain, high-quality cycleways and a low risk of accidents can encourage commuter cycling in both regions. However, heavy traffic (on municipal roads) does not have any significant impact in Flanders, whereas it strongly discourages cycling in Wallonia and Brussels. In Flanders, the high visibility of cyclists in the traffic (because there are such a lot of them) and the presence of appropriate cycling infrastructure probably give commuter cyclists a feeling of personal security and, hence, offset the deterrent effect of traffic volume. Policies in Flanders do indeed provide high-quality infrastructure (e.g. continuous and separate cycleways) and facilities (e.g. changing facilities at work, covered cycle racks) with the intention of improving the safety and convenience of cycling. Flanders also stimulates bicycle use through regulations restricting motorised traffic in urban centres (e.g. through the introduction of traffic calming areas), so that the risk and annoyance of heavy traffic is greatly reduced. Finally, motorists show more respect for cyclists because they often cycle themselves and/or are used to sharing the road with large numbers of cyclists.

The opposite situation is observed in Wallonia and the Brussels region: here, the terrain is more hilly and discourages cycling. Also, motorists are seldom mindful of commuter cyclists

⁹ Commuters with a car at their disposal and attracted by green amenities often try to live on the outskirts of large cities. Public transport in these areas is often poor, and so long commuting journeys by car are common. ¹⁰ The practice of cycling in the company of at least one other person.

and still consider them less important than car drivers (especially in Wallonia). Due to a lack of cycling infrastructure in the Walloon municipalities, the risk of being seriously injured or killed is high (especially in rural areas), and confirms residents' fears of cycling. This is not, however, the case in Brussels, where casualty rates are low (Vandenbulcke et al., 2009); indeed, the urban environment, with its large number of obstacles, forces drivers to reduce their speed.

In Brussels and Wallonia, the provision of an extensive and high-quality cycling network would certainly reduce the numerous fears and safety concerns inhabitants have about cycling. In particular, providing continuous, separate and well-maintained cycle paths could reduce the risk of accidents and mitigate the effects of traffic, as well as improving the general attitude commuters have towards cyclists (e.g. in terms of danger and societal status) (McClintock and Cleary, 1996). It could also reduce the exposure of cyclists to air pollution since even small "separation distances" from the emission source significantly decrease the concentration of ultra fine particles (UFP) (Int Panis et al., 2008; Thai et al., 2008). Cycling networks should hence be planned so that the impact of deterrent variables (e.g. accident risks, slopes, traffic volume, air pollution) is reduced. Our results (Section 6.5.3.) suggest that even small reductions in the daily mileage, the mean slope of the road network, or the risk of accidents could significantly increase bicycle use. This could be achieved by providing 'optimal paths' for cyclists (i.e. alternatives to congested, sloping and/or hazardous roads). These paths could either be existing streets (e.g. quiet residential streets, without parking facilities) or new cycling infrastructure (e.g. constructed along the road). Ideally, planners and engineers should design such paths so that they are separate from road traffic, but still allow cyclists and motorists to see each other, so that inexperienced and 'elderly' cyclists (who may behaviour inappropriately because of their age¹¹) are protected from motorised traffic but do not have an ill-founded feeling of security. Our results also suggest that new cycleways should be made as flat as possible, or at least that any slopes should be long and gentle (so that the physical effort is reduced). For instance, new bridges specifically designed to enable cyclists to bypass dangerous or unpleasant situations should have gentle slopes. Including information about the topography on cycling maps and promoting the use of electric bicycles are other ways of "bypassing" the negative impact of hilly terrain.

The implementation of stricter parking policies and regulation of motorised traffic could also reduce the deterrent effect of high traffic volumes on cycling. Examples of such measures are parking and road capacity limitations (restriction of car use), traffic calming measures, speed limitations, and taxes on automobile ownership/use (Pucher and Dijkstra, 2003; Pucher and Buehler, 2008). The development of appropriate bicycle facilities at the origins and destinations of the trip (e.g. cycle racks and lockers at stations) could also help by increasing users' satisfaction with cycling equipment and, hence, encouraging cycling and its integration with public transport (Martens, 2004, 2007; Pucher and Buehler, 2008).

Lastly, special attention should be paid to traffic education and enforcement, especially in Wallonia where the accident risk is generally higher than in the rest of the country. It is quite striking that, in this region, more than half of all motorists were found to be going over the speed limit on 50 km/h roads, and nearly a quarter were over 60 km/h (2003–2006 period) (BRSI, 2008). Tackling such hazardous driving behaviour would obviously reduce the risk motorists constitute for cyclists.

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¹¹ In particular, reaction time (to sound, light, urgency, etc.) significantly increases with age, and more especially for people over 50 (Der and Deary, 2006; Makishita and Matsunaga, 2008; Fondarai et al., 2009).

7.3. Land-use planning policies: towards compact and mixed-use cities?

Land-use and urban design policies are very important for increasing bicycle use. Our findings suggest that municipalities that are well-equipped (i.e. large and regional towns) and characterised by short commuting distances have high rates of commuter cycling. Large urban areas generally provide high-quality public transport and benefit from the proximity of different activities and the good connectivity between them, so that commuting distances are shorter and more bikeable. As a consequence, promoting dense and mixed-use development (especially in cities) could reduce commuting distances and encourage cycling. Redevelopment of urban areas (i.e. urban regeneration), promotion of bicycle storage facilities in blocks of flats, and financial measures encouraging people to live in cities are some examples of such measures. In the long-run, these measures could not only increase the use of non-motorised and public transport for commuting, but could also mitigate the negative impacts of motorised traffic (air pollution, congestion, noise, etc.) and improve the quality of life in urban areas.

7.4. Strategies to create a supportive environment for cycling

Our findings suggest that bicycle use in a municipality is influenced (through spillover effects) by the levels of cycling in the neighbouring municipalities: a municipality surrounded by others with high levels of cycling is more likely to show high rates of commuter cycling (and vice versa). This indicates that social support for cycling could stem from the neighbourhood. This confirms results obtained at a more disaggregated scale (de Geus, 2007; de Geus et al., 2008). Among other measures, the implementation of a public bicycle sharing system would probably be an efficient way to create such a supportive environment in urban areas (especially in Brussels and Antwerp, where the potential for increasing bicycle use is still large)¹². Finally, high spatial autocorrelation (detected for bicycle use) underlines the importance of an inter-municipal approach, such as has been applied in Flanders through the implementation of a super-local functional cycleway network. This aims at building connections between neighbouring municipalities, and so stimulating utilitarian trips (to work, school and other facilities) (MV, 2006). Such a continuous network is essential in order to turn the bicycle into a more functional and safer mode of transport.

8. Concluding remarks

From the methodological point of view, the aggregate modelling techniques applied in this paper highlight the importance of accounting for multicollinearity, spatial dependence and spatial heterogeneity (i.e. structural instability and heteroskedasticity). These statistical issues should be carefully considered in future research in order to achieve reliable statistical inferences. Spatial autoregressive models appear to be very powerful in eliminating spatial autocorrelation, while the presence of spatial heterogeneity in the data is corrected using White's correction and a spatial regime regression. The results suggest that bicycle use in a

¹² We do not know of any studies of the impact of such systems on commuter cycling. Statistics do however suggest that cities equipped with such a system experience - immediately after the launch and later - a considerable increase in bicycle use (e.g. +80% cycling trips in Lyon, from the launch in June 2005 to May 2009; +70% cycling trips in Paris from the launch in July 2007 to June 2008). Interestingly, in these two cities, most cyclists (70%) use their own bicycle while only 30% (on average) hire a public bicycle (City of Paris, 2007; Greater Lyon, 2009). This suggests that social support for cycling is increased by the system. The increased visibility and better image of cyclists on the "street scene" probably explain a large part of this encouraging effect.

municipality is influenced (positively or negatively) by the neighbouring municipalities, and that different effects exist in the northern (Flanders) and southern (Wallonia and Brussels) parts of Belgium. Pro-cycling strategies should hence be regionally differentiated, without however neglecting inter-regional approaches and exchanges (which are indispensable for promoting bicycle use in Brussels and its periphery).

For transportation planners and policy makers, this research also provides several statistically-based recommendations which may be useful in encouraging commuters to shift from car to bicycle. These measures are, however, generally not efficient when implemented on their own. Planners and policy makers should be aware that only a combination of them (promotional campaigns, improvement of cycling facilities, etc.) will really lead to an increase in cycle commuting. This increase could in turn address environmental, mobility and health problems (and their associated costs) with which our society is faced nowadays. Additionally, it has economic consequences. The lion's share of trips are currently made by car, and our society and its economic activity is becoming more and more car- and fuel-dependent. Increasing the number of commuter cyclists will mean lowering the number of drivers and reducing the dependence of the economy on fuel, which in turn will decrease society's vulnerability to an energy crisis. It is not a matter of chance that the Dutch government invested in cycling infrastructure during the oil crisis of the early 1970s.

References

Anselin, L. (1988). Spatial Econometrics: Methods and Models. Kluwer Academic Publishers, Dordrecht.

Anselin, L. (1995). Local indicators of spatial association-LISA. Geographical Analysis 27, 93-115.

Anselin, L. (1998a). Interactive techniques and exploratory spatial data analysis. In: Longley, P.A., Goodchild, M.F., Maguire, D.J., Wind, D.W. (Eds.), *Geographical Information Systems: Principles, Techniques, Management and Applications*. Wiley, New York.

Anselin, L. (1998b). Exploratory spatial data analysis in a geocomputational environment. In: Longley, P.A., Brooks, S.M., McDonnell, R., Macmillan, B. (Eds.), *Geocomputation, a Primer*. Wiley, New York.

Anselin, L. (2005). *Exploring Spatial Data with GeoDa: A Workbook*. Spatial Analysis Laboratory and Center for Spatially Integrated Social Science. Available at: [http://geodacenter.asu.edu/learning/tutorials]

Anselin, L. (2007). *Spatial Regression Analysis in R: A Workbook*. Spatial Analysis Laboratory and Center for Spatially Integrated Social Science. Available at: [http://geodacenter.asu.edu/learning/tutorials]

Anselin, L., Bera, A.K., Florax, R., Yoon, M.J. (1996). Simple diagnostic tests for spatial dependence. *Regional Science and Urban Economics* 26 (1), 77-104.

Anselin, L., Florax, R. (1995). Small sample properties of tests for spatial dependence in regression models. In: Anselin, L. and Florax, R. (Eds.), *New Directions in Spatial Econometrics*, Springer, Berlin, 21-74.

Anselin, L., Griffith, D.A. (1988). Do spatial effects really matter in regression analysis? *Papers of the Regional Science Association* 65, pp. 11-34.

Anselin, L., Rey, S. (1991). Properties of tests for spatial dependence in linear regression models. *Geographical Analysis* 23, 112-131.

Baller, R.D., Anselin, L., Messner, S.F., Deane, G., Hawkins, D.F. (2001). Structural covariates of U.S. county homicides rates: incorporating spatial effects. *Criminology* 39 (3), 561-590.

Bergström, A., Magnusson, R. (2003). Potential of transferring car trips to bicycle during winter. *Transportation Research Part A* 37, 649-666.

Bivand, R. (2008). Modelling areal data. In: Bivand, R. (Ed.), *Applied Spatial Data Analysis with R*, Springer, New York. Available at: [http://www.springerlink.com/content/978-0-387-78170-9]

BMA (British Medical Association) (1992). Cycling toward Health and Safety. Oxford University Press, London.

BRSI (Belgian Road Safety Institute) (2008). *L'Observatoire pour la Sécurité Routière: Evolution de la Sécurité Routière en Belgique* (2000-2006). IBSR-BIVV, Brussels. Available (in French) at: [http://bivvweb.ipower.be/Observ/FR/bivv_stat_FR_Lowres.pdf]

Cervero, R., Kockelman, K. (1997). Travel demand and the 3Ds: density, diversity and design. *Transportation Research Part D* 2 (3), 199-219.

Chapman, L. (2007). Transport and climate change: a review. Journal of Transport Geography 15, 354-367.

City of Paris (2007). Le bilan des déplacements en 2007 à Paris. L'observatoire des déplacements à Paris, Paris. Available at:

[http://www.paris.fr/portail/deplacements/Portal.lut?page id=9071&document type id=5&document id=64255 &portlet_id=21968]

Curtis, C., Headicar, P. (1997). Targeting travel awareness campaigns – which individuals are more likely to switch from car to other transport for the journey to work? *Transport Policy* 4 (1), 57-65.

de Geus, B. (2007). Cycling to Work: Psychosocial and Environmental Factors Associated with Cycling and the Effect of Cycling on Fitness and Health Indexes in an Untrained Working Population. Ph.D. Thesis in Physical Education, Vrije Universiteit Brussel (VUB), Brussels.

de Geus, B., De Bourdeaudhuij, I., Jannes, C., Meeusen, R. (2008). Psychosocial and environmental factors associated with cycling for transport among a working population. *Health Education Research* 23 (4), 697-708.

de Geus, B., Van Hoof, E., Aerts, I., Meeusen, R. (2008). Cycling to work: influence on indexes of health in untrained men and women in Flanders. Coronary heart disease and quality of life. *Scandinavian Journal of Medicine and Science in Sports* 18 (4), 498-510.

de Geus, B., Joncheere, J., Meeusen, R. (2009). Commuter cycling: effect on physical performance in untrained men and women in Flanders. Minimum dose to improve indexes of fitness. *Scandinavian Journal of Medicine and Science in Sports* 19 (2), 179-187.

Der, G., Deary, I.J. (2006). Age and sex differences in reaction time in adulthood: Results from the United Kingdom health and lifestyle survey. *Psychology and Aging* 21 (1), 62-73.

Dickinson, J.E., Kingham, S., Copsey, S., Pearlman Hougie, D.J. (2003). Employer travel plans, cycling and gender: will travel plan measures improve the outlook for cycling to work in the UK? *Transportation Research Part D* 8, 53-67.

Dobruszkes, F., Marissal, P. (1994). La problématique des déplacements à Bruxelles. *Revue Belge de Géographie* 118 (3), 133-153.

EC (European Commission) (2000). *Villes cyclables, villes d'avenir*. Office des publications officielles des Communautés européennes, Luxembourg. Available at:

[http://ec.europa.eu/environment/archives/cycling/cycling_fr.pdf]

EEA (European Environment Agency) (2007). *Air Pollution in Europe 1990-2004*. Office for Official Publications of the European Communities, Luxembourg. Available at: [http://www.eea.europa.eu/publications/eea report 2007 2]

EROS (Earth Resources Observation and Science Center) (2002). Shuttle radar topography mission (SRTM) – Elevation data set (Belgium). Available at: [http://eros.usgs.gov/]

Federal Police (2000-2002). Bicycle Theft during the Period 2000-2006, on the Zonal and Communal Scales. General Commissioner's Office, Directorate of Operational Police Information, Brussels (available in French and Dutch).

Fondarai, J.-A., Avril, P.-B., Michel, B.-F., Bartolin, R. (2009). Evolution of visual reaction time according to age: a meta-analysis of a total of 1222 cases. *Les cahiers de l'année gérontologique* 1 (1), 3-9.

Gatersleben, B., Appleton, K.M. (2007). Contemplating cycling to work: attitudes and perceptions in different stages of change. *Transportation Research Part A* 41, 302-312.

Greater Lyon (2009). Comptage des vélos – En trois ans, deux fois plus de vélos. Grand Lyon, Communauté urbaine. Available at: [http://www.grandlyon.com/Comptage-des-velos.2231.0.html]

Heinen, E., van Wee, B., Maat, K. (2009). Impact of work-related factors on levels of bicycle commuting. In: 88th Meeting of the Transportation Research Board, 11-15 January 2009, Paper 09-1212, Washington DC.

Hertel, O., Hvidberg, M., Ketzel, M., Storm, L., Stausgaard, L. (2008). A proper choice of route significantly reduces air pollution exposure – a study on bicycle and bus trips in urban streets. *Science of the Total Environment* 389, 58-70.

Hopkinson, P., Wardman, M. (1996). Evaluating the demand for new cycle facilities. *Transport Policy* 3 (4), 241-249.

Hubert, J-P., Toint, P. (2002). La Mobilité Quotidienne des Belges. Namur: Presses universitaires de Namur.

Int Panis, L., De Nocker, L., De Vlieger, I., Torfs, R. (2001). Trends and uncertainty in air pollution impacts and external costs of Belgian passenger car traffic. *International Journal of Vehicle Design* 27 (1-4), 183-194.

Int Panis, L., De Nocker, L., Cornelis, E., Torfs, R. (2004). An uncertainty analysis of air pollution externalities from road transport in Belgium in 2010. *Science of the Total Environment* 334-335, 287-298.

Int Panis, L., Bleux, N., Torfs, R., Mishra, V., de Geus, B., Meeusen, R., Vandenbulcke, G., Thomas, I. (2008). Exposure of cyclists to ultra fine particles. In: *Ninth Highway and Urban Environment Symposium*, Madrid, Spain 9-11 June 2008.

IRCEL-CELINE (Belgian Interregional Cell for the Environment) (2000-2005). Measurements on particulate matter concentrations (PM10). Available at: [http://www.irceline.be/]

Jacobsen, P.L. (2003). Safety in numbers: more walkers and bicyclists, safer walking and bicycling. *Injury Prevention* 9, 205-209.

Jensen, M. (1999). Passion and heart in transport – a sociological analysis on transport behaviour. *Transport Policy* 6, 19-33.

Kingham, S., Dickinson, J., Copsey, S. (2001). Travelling to work: will people move out of their cars. *Transport Policy* 8, 151-160.

Kitamura, R., Mokhtarian, P., Laidet, L. (1997). A micro-analysis of land use and travel in five neighborhoods in the San Francisco Bay Area. *Transportation* 24, 125-158.

Knowles, R.D. (2006). Transport shaping space: differential collapse in time-space. *Journal of Transport Geography* 14, 407-425.

Koetse, M.J., Rietveld, P. (2009). The impact of climate change and weather on transport: an overview of empirical findings. *Transportation Research Part D* 14 (3), 205-221.

Le Gallo, J. (2004). Hétérogénéité spatiale. Principes et méthodes. Economie et prévision 1 (162), 151-172.

Le Gallo, J., Ertur, C. (2003). Exploratory spatial data analysis of the distribution of regional per capita GDP in Europe, 1980-1985. *Papers in Regional Science* 82, 175-201.

LeSage, J.P., Fisher, M.M. (2008). Spatial growth regressions: Model specification, estimation and interpretation. *Spatial Economic Analysis* 3 (3), 275-304.

LeSage, J.P., Pace, R.K. (2009). Introduction to spatial econometrics. Taylor & Francis CRC Press, Boca Raton.

Long, J.S., Ervin, L.H. (2000). Using heteroscedasticity consistent standard errors in the linear regression model. *The American Statistician* 54 (3), 217–224.

Makishita, H., Matsunaga, K. (2008). Differences of drivers' reaction times according to age and mental workload. *Accident Analysis and Prevention* 40 (2), 567-575.

Martens, K. (2004). The bicycle as a feedering mode: experiences from three European countries. *Transportation Research Part D* 9, 281-294.

Martens, K. (2007). Promoting bike-and-ride: The Dutch experience. Transportation Research Part A 41, 326-338

McClintock, H., Cleary, J. (1996). Cycle facilities and cyclists' safety – experience from Greater Nottingham and lessons for future cycling provision. *Transport Policy* 3, 67-77.

Meurs, H., Haaijer, R. (2001). Spatial structure and mobility. Transportation Research Part D 6, 429-446.

Moudon, A.V., Lee, C., Cheadle, A.D., Collier, C.W., Johnson, D., Schmid, T.L., Weather, R.D. (2005). Cycling and the built environment, a US perspective. *Transportation Research Part D* 10, 245-261.

MV (Mobiele Vlaanderen) (2006). Het bovenlokaal fietsroutenetwerk. *Mobiliteitsbrief* 76. Available at: [http://www.mobielvlaanderen.be/convenants/artikel.php?nav=3&mbnr=76&id=430] [Dutch]

Nankervis, M. (1999). The effect of weather and climate on bicycle commuting. *Transportation Research Part A* 33, 417-431.

NIS (National Institute for Statistics) (2000). Downoadable files: Society, mobility and transport. Available (in French and Dutch) at: [http://statbel.fgov.be/figures/download_fr.asp#mob]

NIS (National Institute for Statistics) (2001a). *National Household Survey on Mobility. Realization and Results*. Research contract MD/13/036, FUNDP-GRT-LV-UIA-IW-INS. Belgian Federal Science Policy Office, Brussels. Available (in French) at: [http://www.belspo.be/belspo/fedra/proj.asp?l=en&COD=MD/DD/18]

NIS (National Institute for Statistics) (2001b). Downoadable files. Available (in French and Dutch) at: [http://statbel.fgov.be/figures/download_fr.asp]

NIS (National Institute for Statistics) (2004). Downoadable files: Territory and environment. Available (in French and Dutch) at: [http://statbel.fgov.be/figures/download_fr.asp#1]

NIS (National Institute for Statistics) (2002-2005). Downoadable files: Society, road accidents. Available (in French and Dutch) at: [http://www.statbel.fgov.be/figures/download_fr.asp#acc]

Noël, N. (2003). Formes urbaines, aménagements routiers et usage de la bicyclette. Ph.D. Thesis, Université Laval, Québec (Canada).

Ortúzar, J. de D., Iacobelli, A., Valeze, C. (2000). Estimating demand for a cycle-way network. *Transportation Research Part A* 34, 353-373.

Parkin, J., Wardman, M., Page, M. (2007). Models of perceived cycling risk and route acceptability. *Accident Analysis and Prevention* 39 (2), 364-371.

Parkin, J., Wardman, M., Page, M. (2008). Estimation of the determinants of bicycle mode share for the journey to work using census data. *Transportation* 35 (1), 93-109.

Pikora, T., Giles-Corti, B., Bull, F., Jamrozik, K., Donovan, R. (2003). Developing a framework for assessment of the environmental determinants of walking and cycling. *Social Science & Medicine* 56, 1693-1703.

Plaut, P.O. (2005). Non-motorized commuting in the US. Transportation Research Part D 10, 347-356.

Pooley, C.G., Turnbull, J. (2000). Modal choice and modal change: the journey to work in Britain since 1890. *Journal of Transport Geography* 8, 11-24.

Pucher, J., Buehler, R. (2006). Why Canadians cycle more than Americans: a comparative analysis of bicycling trends and policies. *Transport Policy* 13, 265-279.

Pucher, J., Buehler, R. (2008). Making cycling irresistible: lessons from the Netherlands, Denmark and Germany. *Transport Reviews* 28 (4), 495-528.

Pucher, J., Dijkstra, L. (2003). Promoting safe walking and cycling to improve public health: lessons from the Netherlands and Germany. *Public Health Matters* 93 (9), 1509-1516.

Pucher, J., Komanoff, C., Schimek, P. (1999). Bicycling renaissance in North America? Recent trends and alternatives policies to promote bicycling. *Transportation Research Part A* 33, 625-654.

Ramajo, J., Márquez, M.A., Hewings, G.J.D., Salinas, M.M. (2008). Spatial heterogeneity and interregional spillovers in the European Union: do cohesion policies encourage convergence across regions? *European Economic Review* 52, 551-567.

Richardson, A.J. (2000). Seasonal and Weather Impacts on Urban Cycling Trips. TUTI Report 1-2000. The Urban Transport Institute, Victoria, Australia.

Rietveld, P. (2000). The accessibility of railway stations: the role of the bicycle in The Netherlands. *Transportation Research Part D* 5, 71-75.

Rietveld, P. (2001). Biking and walking: the position of non-motorized transport modes in transport systems. Tinbergen Institute Discussion Paper TI 2001-111/3.

Rietveld, P., Daniel, V. (2004). Determinants of bicycle use: do municipal policies matter? *Transportation Research Part A* 38, 531-550.

Rodríguez, D.A., Joo, J. (2004). The relationship between non-motorized mode choice and the local physical environment. *Transportation Research Part D* 9, 151-173.

Saelens, B.E., Sallis, J.F., Frank, L.D. (2003). Environmental correlates of walking and cycling: findings from the transportation, urban design, and planning literatures. *Annals of Behavioral Medicine* 25 (2), 80-91.

SPW (Service Public de Wallonie) (2008). Le Plan Escargot – un Soutien Financier aux Communes pour Favoriser les Modes Alternatifs de Déplacement. La CeMathèque, Namur.

SSTC (Services fédéraux des Affaires Scientifiques, Techniques et Culturelles) (2001). *Enquête Nationale sur la Mobilité des Ménages : Réalisations et Résultats. Rapport Final.* Contract MD/13/036, FUNDP-GRT-LV-UIA-IW-INS.

Thai, A., McKendry, I., Brauer, M. (2008). Particulate matter exposure along designated bicycle routes in Vancouver, British Columbia. *Science of the Total Environment* 405, 26-35.

Tilahun, N.Y., Levinson, D.M., Krizek, K.J. (2007). Trails, lanes, or traffic: valuing bicycle facilities with an adaptative stated preference survey. *Transportation Research Part A* 41, 287-301.

Titheridge, H., Hall, P. (2006). Changing travel to work patterns in South East England. *Journal of Transport Geography* 14, 60-75.

Vandenbulcke, G., Steenberghen, T., Thomas, I. (2007). *Accessibility Indicators to Places and Transports: Final Report*. Belgian Science Policy and FPS Mobility and Transports, Brussels. Research project AP/02. Available at: [http://www.mobilit.fgov.be/fr/index.htm]

Vandenbulcke, G., Thomas, I., de Geus, B., Degraeuwe, B., Torfs, R., Meeusen, R., Int Panis, L. (2009). Mapping bicycle use and the risk of accidents for commuters who cycle to work in Belgium. *Transport Policy* 16, 77-87. Available at: [doi:10.1016/j.tranpol.2009.03.004]

Van Hecke, E. (1998). Actualisering van de stedelijke hiërarchie in België. *Tijdschrift van het Gemeentekrediet van België*, No. 205, 45–76.

Van Malderen, L., Jourquin, B., Thomas, I., Vanoutrive, T., Verhetsel, A., Witlox, F. (2009). Mobility policies of the companies located in Belgium: are there success stories? In: *Proceedings of the BIVEC-GIBET Transport Research Day* (3rd edition), Belgium, May 27, 2009, Brussels, Vrije Universiteit Brussel (VUB).

van Wee, B., Nijland, H. (2007). Health benefits of cycling. In: *CVS 2007 34th Edition*, Belgium November 22-23, 2007, Antwerpen, Cultureel Congresscentrum Elzenveld.

Verhetsel, A. (1998). The impact of spatial versus economic measures in an urban transportation plan. *Computers, Environment and Urban Systems* 22 (6), 541-555.

Verhetsel, A., Thomas, I., Van Hecke, E., Beelen, M. (2007). *Monografie van het Woonwerkverkeer in Belgïe*. Belgian Science Policy and FPS Mobility and Transports, Brussels.

Wardman, M., Tight, M., Page, M. (2007). Factors influencing the propensity to cycle to work. *Transportation Research Part A* 41, 339-350.

WHO (World Health Organization) (2002a). 30 minutes for a healthy life span. Press release EURO/07/02, Copenhagen and Rome.

WHO (World Health Organization) (2002b). A Physically Active Life through Everyday Transport, with a Special Focus on Children and Older People, and Examples and Approaches from Europe. Regional Office for Europe, Copenhagen.

Witlox, F., Tindemans, H. (2004). Evaluating bicycle-car transport mode competitiveness in an urban environment: an activity-based approach. *World Transport Policy and Practice* 10 (4), 32-42.

Woodcock, J., Banister, D., Edwards, P., Prentice, A.M., Roberts, I. (2007). Energy and transport. *The Lancet* 370, 1078-1088.

Zahran, S., Brody, S.D., Maghelal, P., Prelog, A., Lacy, M. (2008). Cycling and walking: explaining the spatial distribution of healthy modes of transportation in the United States. *Transportation Research Part D* 13, 462-470.

Appendices

Appendix A: Variables used: description, units of measurement and data sources

| Group | Variable | Description | Units | Source |
|---------------------------------------|--|---|--------------------------|----------------------------------|
| Dependent variable | | | | |
| | Cycle commuting (y) | Proportion of commuting by bicycle | Percent | 2001 Census |
| Independent variable | es | | | |
| Demographic data | Working men | Percentage of working people that are men | Percent | NIS (2001b) |
| | Age 1 (< 25 years) | Percentage of working people being less than 25 years of age | Percent | 2001 Census |
| | Age 2 (45-54 years) | Percentage of working people being between 45 and 54 years of age | Percent | 2001 Census |
| | Age 3 (> 54 years) | Percentage of working people being more than 54 years of age | Percent | 2001 Census |
| | Young children | Percentage of working households (i.e. with one or more working parents) having one or more young children (i.e. being between 0 and 5 years of age) | Percent | Own computation from 2001 Census |
| Socio-economic data | Education 1 (primary degree) | Percentage of working people having a primary degree as highest qualification | Percent | 2001 Census |
| | Education 2 (secondary degree) | Percentage of working people having a secondary degree as highest qualification | Percent | 2001 Census |
| | Education 3 (higher/university degree) | Percentage of working people having a higher/university degree as highest qualification | Percent | 2001 Census |
| | Income | Median income | Euro (.10 ³) | NIS (2001b) |
| | Bad health | Percentage of inhabitants feeling they have a bad state of health | Percent | 2001 Census |
| | Car availability | Percentage of households that do not own any car | Percent | NIS (2001b) |
| Environmental and policy-related data | Population density | Population density | Inhabitants/km² | NIS (2001b) |
| | Jobs density | Jobs density | Jobs/km² | NIS (2001b) |
| | Commuting distance | Average commuting distance of working people, by day | Kilometer | 2001 Census |
| | Minimum distance to the closest town | Minimum network distance to the closest town. Town = large town, regional town, and small town which is well-equipped in facilities (see Vandenbulcke et al. (2009) for more details) | Kilometer | Vandenbulcke et al. (2007) |
| | Share of commuters, d < 10 km | Percentage of commuters that live no further than 10 km from their workplace | Percent | 2001 Census |
| | City size | Urban hierarchy of Belgian municipalities (largest towns = 1; regional towns = 2;; smallest towns = 8) | 0-8 | Van Hecke (1998) |
| | Urbanisation | Percentage of urban area in the municipality | Percent | NIS (2004) |
| | Forests | Percentage of forest area in the municipality | Percent | NIS (2004) |
| | Agriculture | Percentage of agricultural area in the municipality | Percent | NIS (2004) |
| | Public services | Percentage of surface dedicated to public services (e.g. administrations, schools) in the municipality | Percent | NIS (2004) |
| | Recreational areas | Percentage of surface dedicated to recreational activities (e.g. parks, sport terrains) in the municipality | Percent | NIS (2004) |
| | Slopes | Mean slope along the municipal road network (excepted motorways and main | Degree | Own computation from EROS data |

| | | express roads) | | (2002) |
|---|---|---|---|---|
| | Cycling facilities unsatisfaction | Percentage of households estimating they have low-quality cycling facilities located in their neighbourhood | Percent | 2001 Census |
| 1 | Bicycle theft | Average annual number of bicycle thefts | Bicycle thefts | Federal Police (2000-2002) |
| | Risk of bicycle theft | Average annual number of bicycle thefts, divided by the total number of cyclists in the municipality | Number of bicycle thefts per cyclist | Own computation from Federal Police data (2000-2002) and 2001 Census |
| , | Accident risk | Average number of victims (cyclists) of accidents per 100,000 bicycle minutes (i.e. travelled on a bicycle) | Victims (cyclists) per 100,000 minutes | Own computation from NIS data (2002-2005) and 2001 Census |
| , | Air pollution | Mean concentration of particulate matter (PM10) | Microgram/m³ | Own computation from IRCEL- CELINE data (2000-2005) |
| i | Traffic volume 1 (regional network) | Number of vehicles-km (.10 ⁶) by kilometer of regional road | 10 ⁶ vehicles-km by kilometer of network | FPS Mobility and Transports, 2000 |
| 1 | Traffic volume 2 (municipal network) | Number of vehicles-km (.10 ⁶) by kilometer of municipal road | 10 ⁶ vehicles-km by kilometer of network | FPS Mobility and Transports, 2000 |

Appendix B: Basic statistics and bivariate correlations with the proportion of commuting by bicycle at the scale of the municipalities (N = 589)

| Variables | Mean | Standard Dev. | Min | Max | Correlation with <i>y</i> | Units |
|--|-------|---------------|------|---------|---------------------------|-----------------|
| Dependent variables | - | - | | - | | |
| Share of commuter cyclists | 4,6 | 4,6 | 0,0 | 21,7 | 1,00*** | Percent |
| Independent variables | • | | | - | | |
| Working men | 57,6 | 2,0 | 50,7 | 64,6 | n.s. | Percent |
| Age 1 (< 25 years) | 10,0 | 1,9 | 5,2 | 17,5 | 0,54*** | Percent |
| Age 2 (45-54 years) | 23,5 | 2,4 | 15,7 | 42,4 | -0,39*** | Percent |
| Age 3 (> 54 years) | 6,9 | 1,5 | 3,9 | 15,3 | -0,30*** | Percent |
| Young children | 20,7 | 2,7 | 10,5 | 30,6 | -0,39*** | Percent |
| Education 1 (primary degree) | 6,0 | 1,9 | 2,0 | 15,3 | n.s. | Percent |
| Education 2 (secondary degree) | 57,5 | 7,3 | 25,8 | 70,3 | 0,21*** | Percent |
| Education 3 (higher/university degree) | 36,6 | 8,4 | 15,3 | 71,8 | -0,20*** | Percent |
| Income (.10³) | 19,4 | 2,0 | 13,4 | 25,1 | 0,25*** | Euro |
| Bad health | 24,1 | 5,0 | 15,1 | 39,4 | -0,58*** | Percent |
| Car availability | 18,1 | 6,9 | 8,1 | 57,1 | -0,25*** | Percent |
| Population density | 675,6 | 1735,7 | 21,4 | 19128,6 | 0,28*** | Inhabitants/km² |
| Jobs density | 203,6 | 725,9 | 1,3 | 8342,1 | 0,38*** | Jobs/km² |
| Commuting distance | 22,6 | 5,7 | 10,2 | 42,7 | -0,54*** | Kilometer |
| Minimum distance to the closest town | 14,7 | 12,2 | 0,0 | 85,8 | -0,26*** | Kilometer |
| Share of commuters, d < 10 km | 35,9 | 11,3 | 12,8 | 67,1 | 0,46*** | Percent |
| City size ^a | 6,3 | 1,5 | 1,0 | 8,0 | -0,23*** | 0-8 |
| Urbanisation | 28,4 | 19,5 | 4,7 | 99,5 | 0,34*** | Percent |
| Forests | 14,3 | 16,2 | 0,0 | 74,0 | -0,33*** | Percent |
| Agriculture | 57,3 | 21,2 | 0,5 | 93,6 | 0,09** | Percent |
| Public services | 1,0 | 1,7 | 0,0 | 22,9 | 0,17*** | Percent |
| Recreational areas | 2,0 | 2,4 | 0,1 | 15,9 | 0,12*** | Percent |
| Slopes | 2,8 | 2,0 | 0,7 | 10,8 | -0,77*** | Degree |
| Cycing facilities unsatisfaction | 65,1 | 18,4 | 24,6 | 95,8 | -0,82*** | Percent |

| Bicycle theft | 56,4 | 166,8 | 0,0 | 2451,7 | 0,75*** | Bicycle thefts |
|---|------|-------|------|--------|----------|--|
| Risk of bicycle theft | 8,9 | 5,8 | 0,0 | 33,0 | n.s. | Number of bicycle thefts per cyclist |
| Accident risk | 0,3 | 0,5 | 0,0 | 7,0 | -0,32*** | Victims (cyclists) per 100,000 minutes |
| Air pollution | 29,3 | 4,2 | 20,6 | 40,8 | 0,23*** | Microgram/m³ |
| Traffic volume 1 (regional network) | 3,1 | 1,9 | 0,0 | 14,0 | 0,31*** | 10 ⁶ vehicles-km by kilometer of network |
| Traffic volume 2 (municipal network) | 0,2 | 0,2 | 0,0 | 1,4 | 0,12*** | 10 ⁶ vehicles-km by kilometer of network |

^{**} Significant at the 95% level
*** Significant at the 99% level
n.s.: not significant
Italic: variables logarithmically transformed

a Spearman correlation is computed for the 'city size' variable only

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